

# A Transitionless Lattice for the Fermilab Main Injector

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## Abstract

Medium energy (1 to 30 GeV) accelerators are often confronted with transition crossing during acceleration. A lattice without transition is presented, which is a design for the Fermilab Main Injector. The main properties of this lattice are that the  $\gamma_t$  is an imaginary number, the maxima of the dispersion function are small, and two long-straight section with zero dispersion.

## I. Introduction

Most medium energy proton accelerators exhibit transition between injection and the end of the acceleration cycles. There are many unfavorable effects which can occur during and after transition[1]. For example, the momentum spread of a bunch around transition can become so large that it exceeds the machine momentum aperture and beam loss occurs[2]. There is little or no Landau damping against microwave instability near transition. As a result, the bunch area grows due to internal space-charge force as well as external beam-pipe wake forces. Particles with different momenta cross transition at different times leading to longitudinal distortions as well. The transition gamma for a particle with momentum  $p$  is defined as  $1/\gamma_t^2 = (dC/C)/(dp/p)$ , where  $C$  is the total path length of the particle around the accelerator. One way to avoid transition is to make  $1/\gamma_t^2$  less than zero; or  $dC/(dp/p) = \sum_i D_i \theta_i \leq 0$ , where  $\theta_i$  is the bending angle of the dipole at the position  $i$ , while  $D_i$  is the dispersion at the same location[3]. In Sect. II, the design method of such a lattice is reviewed. In Sect. III, a design for the Fermilab Main Injector is presented. We call this design an "advanced"  $\gamma_t$  lattice because it has a better compaction factor with respect to the one previously presented[4]. In Section IV, the chromaticities of the lattice are discussed and the dependence on momentum is analyzed. The tunability of the lattice, the betatron function and the tune dependence on the gradient errors in the main quadrupoles, the misalignment errors, as well as the study of the dynamical aperture will be given in a separate paper[5].

## II. Review of the Design Method

The horizontal dispersion function is presented in a normalized Floquet's coordinate system as  $\xi = D/\sqrt{\beta} = A \sin \phi$  and  $\chi = D'\sqrt{\beta} + \alpha D/\sqrt{\beta} = A \cos \phi$ , where  $D$  and  $D'$  are the dispersion and the slope of the dispersion function, respectively, while  $\beta$ ,  $\alpha$ , and  $\phi$  are the Twiss parameters[6]. To provide an average negative value of the horizontal dispersion through the

dipoles, most dipoles should be placed in a lattice with negative dispersion (within the third and fourth quadrants of the  $\chi$ - $\xi$  space.) The basic block of the imaginary  $\gamma_t$  lattice is presented in the normalized dispersion space in Fig. 1.

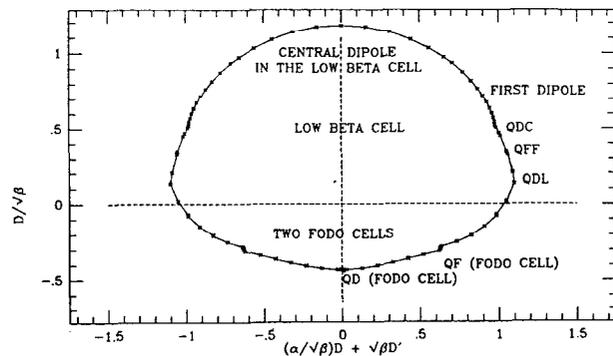


Fig. 1. Normalized horizontal dispersion function in the basic block of the imaginary  $\gamma_t$  lattice.

The second-order inhomogeneous differential equation of motion can be represented as propagation of the betatron phase along a circle without changing the amplitude  $A$  for particle motion throughout all elements except the dipoles. In the thin element approximation, the motion through a dipole is presented by a vector parallel to the  $\chi$ -axis with a length equal to  $\Delta\chi \cong \theta\sqrt{\beta}$ . When the dipole is thick, a change in the coordinate  $\chi$  becomes a smooth curved function because of the phase advance through the dipole. As an approximation, the kick in the slope of the dispersion function is placed at the center of the dipole and the phase advance is taken into account from the dipole beginning to the center and from the center to the other end of the dipole. This method provides a very intuitive approach to the lattice design. The motion of a particle through the two FODO cells (12 dipoles—3 per half cell) is presented in the third and the fourth quadrants of the normalized space in Fig. 1. The second part of the normalized dispersion plot, located mostly in the first and second quadrant of the  $\xi$ - $\chi$  space, represents a motion through the low-beta insertion cell. The major role of this cell is to provide the phase difference necessary to close the betatron functions, including the dispersion function to the beginning of the FODO cell. The low-beta insertion is symmetric and is defined with two quadrupole triplets. For compactness, the first D-quad of the first triplet replaces the last D-quad in the FODO cell which was present in the previous design. Although there are three dipoles in the middle of the low beta insertion cell, their influence on the dispersion function is very small due to the small values of  $\beta_x$  in this region. As a result, horizontal kicks can hardly be seen in the low-beta region in Fig. 1.

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### III. Lattice Properties

The design of the imaginary  $\gamma_t$  lattice in this example represents a possible solution for the 150 GeV future Main Injector in Fermilab. The transition gamma is an imaginary number,  $\gamma_t = i24.37$ . The lattice has to follow many geometrical constraints due to the limited site space. It also has to follow the shape of the tunnel of the existing FODO-cell-based design. There are 302 dipoles available; 8 straight sections at specific locations (two of which need to have zero dispersion), and the total length has to be exactly 3319.4186 meters.

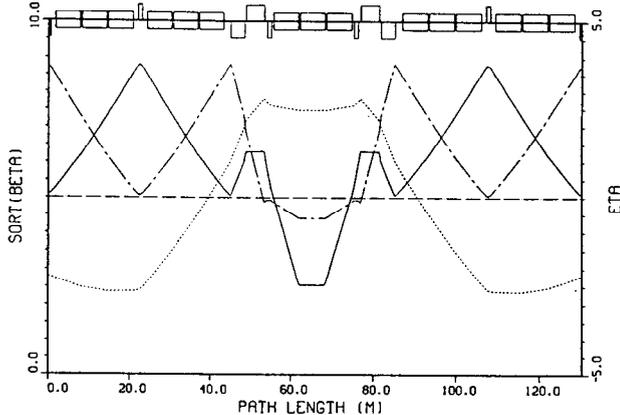


Fig. 2. The betatron and dispersion functions within the regular block (BLR) of the imaginary  $\gamma_t$  lattice. The long-straight section block (BLS) is very similar, just with the 3rd, 4th, 7th, 8th, 9th, 12th, and 13th dipoles removed.

The whole ring consists of three types of blocks. The basic block "BLR" (Fig. 2) consists of two  $60^\circ$  FODO cells containing 12 dipoles and a low-beta insertion containing 3 dipoles. The gradient of every quadrupole in the ring is  $\pm 220$  kG/m. The maximum values of the horizontal and vertical betatron functions in the FODO cell are 77.42 m and 76.78 m, respectively. The quad lengths are 1.0325 m while the dipole length is defined as 6.096 m by the prototype magnet already built. The maximum and minimum of the dispersion function within the whole ring are  $-2.77$  meters and  $+2.82$  meters. Two FODO cells in a row are connected to the low-beta insertion where both betatron functions have minimum values in the center [ $(\beta_x)_{\min} = 4.3$  m]. The low-beta insertion is defined with two triplets. The first quad of length 3.34 m in the triplet replaces the last quadrupole of the FODO cell which was present in the previous design. The central quad in the triplet has the longest length of 4.64 m, while the last quad is just a usual FODO quad.

There are 6 straight-section blocks "BLS" designed to be used for extraction and injection purposes. There are eight dipoles in each of these blocks. To match this block to the other blocks, the lengths of the first two quads in the low beta insertion cell are slightly different. The first quad is 2.84 m long while the middle one is 4.06 m. The last quad nearest to the low-beta region is the same as a usual FODO quad. There is a 24.1 m available drift for the extraction magnets. Two additional 7.69 meter drifts, designed for the kicker magnets or the electrostatic septa, are located  $90^\circ$  upstream and downstream of the extraction magnet position. The low values of both betatron functions at the extraction magnets in the low-beta insertion imply smaller beam size during the fast extraction. For the slow extraction, it is possible to operate the triplet quads on a different circuit to provide for the necessary high value for

one of the betas.

The zero-dispersion straight section is defined within the third block "BLN", which is shown in Fig. 3. This block contains 18 dipoles and has a total of a 72 m straight section with zero dispersion. Again, to provide a perfect match to the other blocks the lengths of quads in the low-beta insertion cell are slightly different. The three quads in the triplet have lengths 2.37 m, 4.13 m, and 1.47 m. The zero-dispersion part of the block is designed mostly with FODO cells and is reserved for installation.

The blocks are perfectly matched for the  $\beta$ 's,  $\alpha$ 's, and dispersion at the center of the D-quad in the middle of the FODO-cell section, so that the blocks can be shuffled in any order provided that geometric closure is retained. For this design, the arrangement is  $2(BLS, BLN, BLS, 6(BLR), BLS, BLR)$ . The differences in lengths between the low-beta quads of different blocks may be accommodated with power supply controls, (special shunt supplies on the same bus).

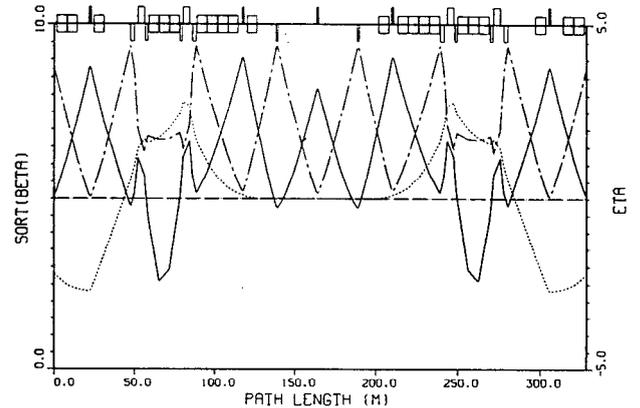


Fig. 3. The betatron and dispersion functions within the block (BLN) with zero-dispersion straight of the imaginary  $\gamma_t$  lattice.

### IV. Chromaticities and Momentum Dependence

The natural chromaticities of this imaginary  $\gamma_t$  example are  $\xi_x = -26.02$  and  $\xi_y = -23.95$ , of the same magnitude as  $|\gamma_t|$ . The horizontal and vertical tunes are 19.714 and 14.188, respectively. The chromaticity sextupoles  $S_F$  are located at the FODO horizontal focussing quads where the horizontal dispersion has negative values of  $-2.6$  m and  $\beta_x = 77.6$  m, while the  $S_D$  are at the defocusing quads where the dispersion is  $-2.2$  m and  $\beta_y = 75.9$  m. The integrated strength of the sextupoles, at a momentum of 150 GeV/c, to compensate for the natural chromaticities are  $k_{sf} = -0.056 \text{ m}^{-2}$  and  $k_{sd} = +0.126 \text{ m}^{-2}$ , respectively. These strengths correspond to pole-tip fields of 1.74 and 3.49 kG, respectively, at 150 GeV for sextupoles of length 20 cm and aperture 5 cm in radius. There are only 44  $S_F$ 's and 22  $S_D$ 's, so they are rather strong and introduce quite large nonlinearities, which must be counteracted by the introduction of a family of harmonic sextupoles in order to achieve a large dynamical aperture. The latter will be studied in a separate paper[5].

The betatron functions dependence on momentum of the chromaticity compensated lattice were examined with two computer programs, SYNCH and TEVLAT. The momentum offsets were introduced in small steps within a range of  $\Delta p/p = \pm 2\%$  although the estimated momentum spread in the future Main